

Observational Studies

Introduction to Quantitative Social Science

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Review of Randomized Control Trials

- Fundamental problem of causal inference:
 - Comparison between factual and counterfactual
 - Counterfactuals are not observed
- Solution: **Randomized controlled trials** (RCTs)
 - Treatment and control groups *identical on average*
 - Similar in all (observed and unobserved) characteristics
- Difference in average outcome between the two groups as an estimate of **Sample Average Treatment Effect** (SATE):

$$\text{difference-in-means estimator} = \frac{1}{n_1} \sum_{i=1}^n T_i Y_i - \frac{1}{n - n_1} \sum_{i=1}^n (1 - T_i) Y_i$$

$$\text{SATE} = \frac{1}{n} \sum_{i=1}^n \{Y_i(1) - Y_i(0)\}$$

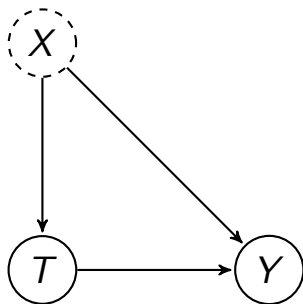
- Examples of RCTs:
 - Causal effect of race on employment prospect
 - Causal effect of naming-and-shaming on turnout

Observational Studies

- Often, we can't randomize treatment for ethical and logistical reasons: e.g., smoking and lung cancer
- Observational studies: naturally assigned treatment

- Better **external validity** for generalization beyond experiment
- Weaker **internal validity**:
 - pre-treatment variables may differ between treatment and control groups
 - **confounding bias** due to these differences
 - **selection bias** from self-selection into treatment
 - **statistical control** needed
 - **unobserved confounding** poses a threat

Confounding



- Key assumption “**Unconfoundedness**”: treatment and control groups comparable with respect to everything other than treatment
- How can we find a good comparison group?

Minimum Wage and Unemployment

- How does the increase in minimum wage affect employment?
- Current debate: federal minimum wage increase
- Many economists believe the effect is negative
 - especially for the poor
 - also for the whole economy
- Hard to randomize the minimum wage increase
- Two social scientists tested this using fast food chains in NJ and PA
- In 1992, NJ minimum wage increased from \$4.25 to \$5.05
 - Neighboring PA stays at \$4.25
 - Observe employment in both states before and after increase
- NJ and (eastern) PA are similar
- Fast food chains in NJ and PA are similar: price, wages, products, etc.
- They are most likely to be affected by this increase

Name	Description
<code>chain</code>	name of fastfood restaurant chain
<code>location</code>	location of restaurants (<code>centralNJ</code> , <code>northNJ</code> , <code>PA</code> , <code>shoreNJ</code> , <code>southNJ</code>)
<code>wageBefore</code>	wage before the minimum wage increase
<code>wageAfter</code>	wage after the minimum wage increase
<code>fullBefore</code>	number of fulltime employees before the minimum wage increase
<code>fullAfter</code>	number of fulltime employees before the minimum wage increase
<code>partBefore</code>	number of parttime employees before the minimum wage increase
<code>partAfter</code>	number of parttime employees before the minimum wage increase

```
minwage <- read.csv("data/minwage.csv")
dim(minwage)

## [1] 358 8
```

Did the Minimum Wage Law Affect the Wages in NJ?

- Subset the data into NJ and PA

```
minwageNJ <- subset(minwage, subset = (location != "PA"))  
minwagePA <- subset(minwage, subset = (location == "PA"))
```

- Compute the proportion of restaurants whose wage is less than \$5.05

```
mean(minwageNJ$wageBefore < 5.05) # NJ before  
## [1] 0.911  
mean(minwageNJ$wageAfter < 5.05) # NJ after  
## [1] 0.00344  
mean(minwagePA$wageBefore < 5.05) # PA before  
## [1] 0.94  
mean(minwagePA$wageAfter < 5.05) # PA after  
## [1] 0.955
```

Are the NJ and PA Restaurants Comparable?

- Average wages before the increase of minimum wage:

```
mean(minwageNJ$wageBefore)
## [1] 4.61
```

```
mean(minwagePA$wageBefore)
## [1] 4.65
```

- Prior proportion of fulltime employment:

```
minwageNJ$fullPropBefore <- minwageNJ$fullBefore /
  (minwageNJ$fullBefore + minwageNJ$partBefore)
minwagePA$fullPropBefore <- minwagePA$fullBefore /
  (minwagePA$fullBefore + minwagePA$partBefore)
mean(minwageNJ$fullPropBefore)
## [1] 0.297
mean(minwagePA$fullPropBefore)
## [1] 0.31
```


Cross-section Comparison

- Compare NJ and PA using the data after the increase
- The treatment and control groups are assumed to be identical on average in terms of all confounders
- What confounders are missing from the data?
- Compute the proportion of fulltime employees after the increase:

```
minwageNJ$fullPropAfter <- minwageNJ$fullAfter /  
(minwageNJ$fullAfter + minwageNJ$partAfter)  
minwagePA$fullPropAfter <- minwagePA$fullAfter /  
(minwagePA$fullAfter + minwagePA$partAfter)
```

- The estimated SATE:

```
mean(minwageNJ$fullPropAfter) -  
  mean(minwagePA$fullPropAfter)  
## [1] 0.0481
```

Before-and-after Comparison

- **State-specific confounders** for cross-section comparison
- Compare NJ before and after
- What might be **time-varying confounders**?

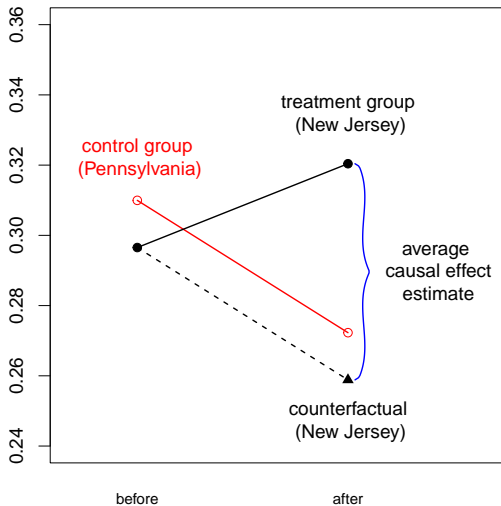
```
NJdiff <- mean(minwageNJ$fullPropAfter) -  
          mean(minwageNJ$fullPropBefore)  
NJdiff  
## [1] 0.0239
```

Difference-in-Differences

- Key Idea: use PA before-and-after difference to figure out what would have happened in NJ without the increase
- NJ before-and-after difference addresses within-state confounding
- **Parallel time trend assumption**
- Estimate the **sample average treatment effect for the treated (SATT)**
- The SATE of minimum wage increase in NJ

```
PAdiff <- mean(minwagePA$fullPropAfter) -  
  mean(minwagePA$fullPropBefore)  
NJdiff - PAdiff  
## [1] 0.0616
```

Visualizing Difference-in-Differences



Summary of 3 Identification Strategies

1 Cross-section comparison

- Compare treated units with control units after the treatment
- Assumption: the treated and control units are comparable
- Possible unit-specific confounding

2 Before-and-after comparison

- Compare the same units before and after the treatment
- Assumption: no time-varying confounding

3 Difference-in-Differences

- Assumption: parallel time trend
- Under this assumption, it accounts for both unit-specific and time-varying confounding

Neither approach is best. They require different assumptions.